Heads (RT) Red f 0 Black equivalet (RI) (RI) (Rominou) Jailo (By) defital 0 0 + B 0 Dangers race to insom of local Cadillac dealer dight then mine?

Strike (p) Wait Wait P, 9 known U,, V, U12, 1/21 within intervals. Strike (9) 21 , 1/2 US Moals: 3) raise u, (but may lower of, lever of, liver rain p) & pears, cold wer, limited were, accidents, budget b) raine U, (but ray raine V2, due lower of, luce raine p) (or: may raise Uz, the enough so that "21' > "21 and military outcome so that p is lowered, so that p is raised; may also raise 9 - raising P. ) C) raise U (see above of though mitigated if Uz is also raised).

To there U, d) lower p (but may lower U, ) raise: V(Wait) - V(Stike) = (V, -V, ) - 9(V, -V, 2) 50 critical risk 9: V11-V21 V4 - V12 US critical risk of. 0, - 021 0, - 0,2 -100, -20 \quad \q 1) alternative postures: 0,0 P= = -20,-100 V(wait) - V(8tile)= "Unstable" (V, - V, ) - 9" (V, - V, ) if 9 = 0, Thi = 20 0,0 -100, -80 9 · 4 p = 4 -80,-100 V(Wait) - V(Stile) - 80 if 9=0 "Stable" (but effect on o; ?)

SHIFT FROM (2) to (6) MAY REPRESENT HIGHER BUDGET: "ARMS RACE"
LIKEWISE FROM (6) TO (2) MAY REPRESENT "DISARMAMENT."

2) Strategic equivaluse:

-80,-100

eithe: 2) 50 AICBM Vs. Polaris

CO band on evocuation + blast shitters

or US C+C vulnuable; or US warning degraded.

(3) Civil Defence: (to say that given clarge in US payoffs will someting about:

"provole" SU attack, or raise p, is to say: (1) q is smarting to clarge on US payoffs, here on p;

2) remarking of q to clarge in p; (3) sinsituity of p to clarge in q p; 4) SU payoffs: p.

0,0 -100, -80 or objecting 0,0 -150, -100

Clarge to: 0) loc + blast + fellent objecting: 0,0 -40

payoffs 0, -60 p some lower (somewhat)

6) fall-art: objecting 0,0 -40

hayoffs: 0 -60 p high

Note: UN-M utilitis: different between 40 -150 million dead may not be "worth" a war "\$ i.e. U(40) = U(0) + p.U(-150) only if p > .6

BUT IT IS NOT "SMALL" or high

CD cont:

A p is lowered, this will raise q: but how much?

and how sensitive is SU decision: how low is p??

2.8. Low high is V; compared to V,?

4

100 MT weapon.

und in 1st strike -60, -100

Aidden, 0,0 -60,-800

(3) Central was tactics (go "swithin" u and v )

Bath spann war: (see (1))
Bath control 1st stile, spann second:

0,0 -

Bath control: 0,0

6 Berlin: do we want of even if y, is lowered deasticely? US monopoly, 0, 0 -15, -100  $\frac{2}{9} = 1$ -10, -100  $\frac{2}{3}$ US Jyh I ligh: V(Wait) - V(Stale) = (100) - 9(0) = 100 But US Type II also high: U(W)-U(S) = (10) - p(15) 50 determe was "unuliable"; unstable to shipts down in un or up in p. The BU acquired capability to hit US bases in Emope + NATO allies 0,0 -30,-80  $\hat{q} = \frac{8}{9}$ -15-20, -90 P= 1-3 US Type I down slightly US Type I dep or down (we had new meson to sticke) 50 chility to lit US (small, embruable) 3,6 -60,-80  $\hat{q} = \frac{1}{3} + \frac{6}{7} - 1$ -40,-60-90  $\hat{p} = \frac{1}{3} + \frac{2}{3}$ US Type I down somewhat, but still high 50 Jupe Is up greatly i not so much in \$ but in sensitivity to drops in U, i. e. Us Type II down slarply; though not "vanished," for big drops

in 4, contained with moderately high p.

D) Wait 0,0 -30,20

NATO Nail 0,0 -60, 20

US doubt - 75, 15

Stile

US does -90, -60

Worst NATO from if SU threature / gestures to go to british wor a) SU night not believe US Strike, so would move.

6) US would Strike, if any fighting developed.

Hence, NATO kreferred policy:

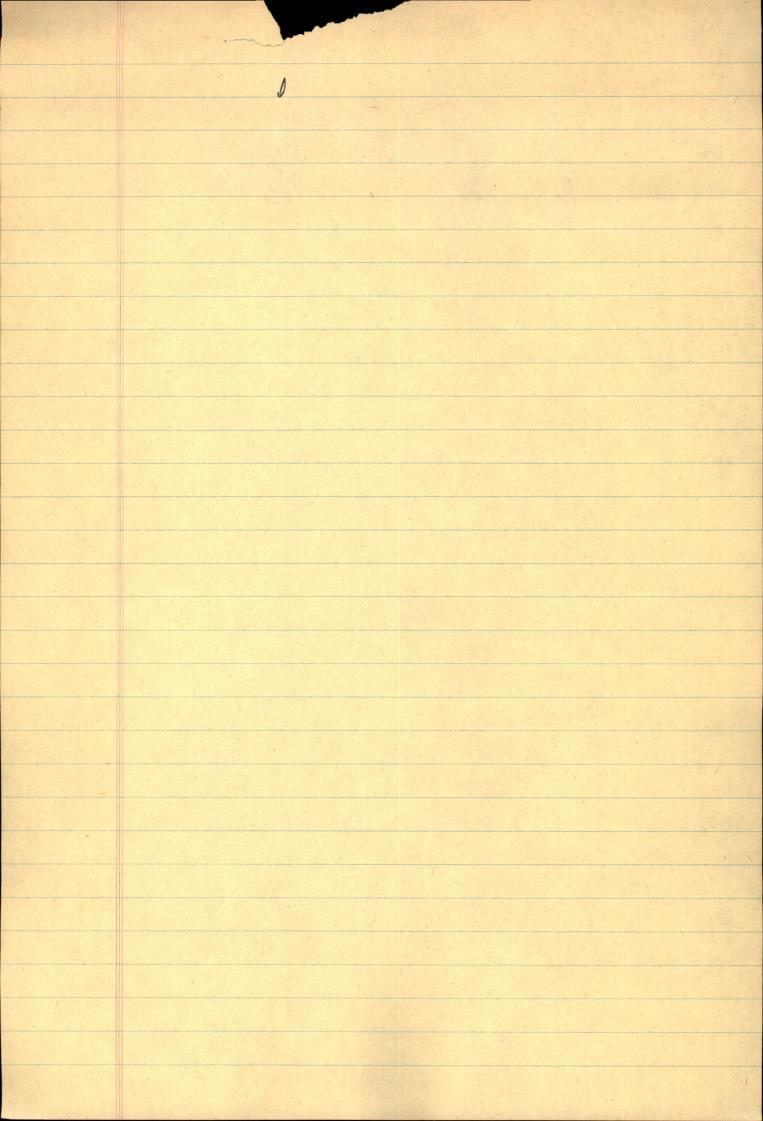
3) make counter threat of US stile as credible as possible (lower raise Uz,) and as frighting (lower V12; generally they prefer this; but want to seem SU without encouraging US)

b) Make sure no fighting develops: negotiate, esp. if wit of fighting booms.

Raising U, will viewer US Type II, in short-run; but it will viewer effectiveness of SU Threats, if NATO doesn't believe that SU "really" believes US will 60; but NATO does believe.

(e.g. US costabled won talk may commisse NATO US was to GO; but they for it won't commisse SU.)

Long. run: 0,0 -60,20
Commutail -10,-20



## Agnorane · Dicision

to their various cusuratarees, what to do. Specifically: when you don't know helat will happen when you take a particular action.

Know helet will dappen who you take a particular action.

"Don't know"; I wish to be more precisety. But what I want to

take about was vagueness is precisely what I want to take about;

and, if I can, I want to talk about if precisely.

How is it reasonable to act when the consequences of your acts! are not menty uncertain but are extremely vague? What does this mean ? How can we identify, to measure, express vagueness; and what implemed does it have on decision. Suppose we can say, meaningfully, that some actions are much now and ignores than ather; Is the a different that notes a different?

- 2. a conflicte theory of cation under uneutrity shists: Ramy.

  Man belows when he stops to think "as if" he abuyed

  Burnalli principle; assigned numbers,...
- 3. Moreover, since this is mornetime, proposents recommend that "you" not only behave "as if" you did this, but that you do just that; R+S.
- 4. What if, when you ask yourself your apinions, you get no answer?
  you get served answers, and when you ask how to compen them,
  ike
  E.g. you've the Rassislet, and the USIB splits?
  - "nost occuptable" one ( any these that are not contradicted by definite opinion); iny one of them "expresses" definite opinions ( iso. before,); but "differe" one las property of "letting sample decide"— which "it will do anyway" if it's big wargh.

5. S, AF, R+S, G paint at it may not make any different which prior dist you was. But somtions it will. Newtlebra, you must act "as if" you had definite opinions - thy gain rules, questions to ask yourself - That will gueste a dist. even who your mind is vague.

Why? Because attenuise you would violate axions; which,
they conjecture—you wouldn't want to do if you stopped to Think.

6. Suppose you did also Bemaille principle; if we know one variable we could measure the aller. Bayes, VN-M. Ransey: assure meither, derine both, starting with special choices: 0, 1 payoff; if we assure Bernalli principle.

E F ENF FOE ENF ENF I I O I O T O I I O

INI => E>F

Build up "body of closes" like this, get an inferred "body of beliefs."
Will it be "consistent" with axions of genel prote?
Will it be true that: E>F, F>G >> E>G

E>FOE(F?

Seppone 1 0 0

E>F, but E>F! But this is ruled out by P2.

Literia: \$10 0 0 \$100 0 P4

· 0 0 E>F, F>G,

A Confining E

I 20 0

10 -10

II 10 10

0 0

If we tale regulo: I' 0 10

 $\mathbb{Z}'$  10 0

is that I offers a definite outcome, I offer two possible outcomes, mentain.

assignment of tilities indicate (only) that this
doesn't make a difference when for (E) = \( \forall \) (more grandly:

I E I i II). But that doesn't man the difference
is involved to behavior for all E: though assisteriorfly
that riteria (as does minimal regret). This seems most
psychologically unsound in just those situations (of high ignorance)
when minimal regret is proposed.

axioms infly that: I 10 0 -10 on I 3 & 5

I 0 0 0 II 6 5

II -10 0 10 II C 3

 $T: \mathbb{T}: \mathbb{T}$  for some  $E \Longrightarrow pr(E) = \frac{1}{2}$  and  $v(b) = \frac{v(a) - v(c)}{2}$ 

and => for all E, not (I > I and I > III)

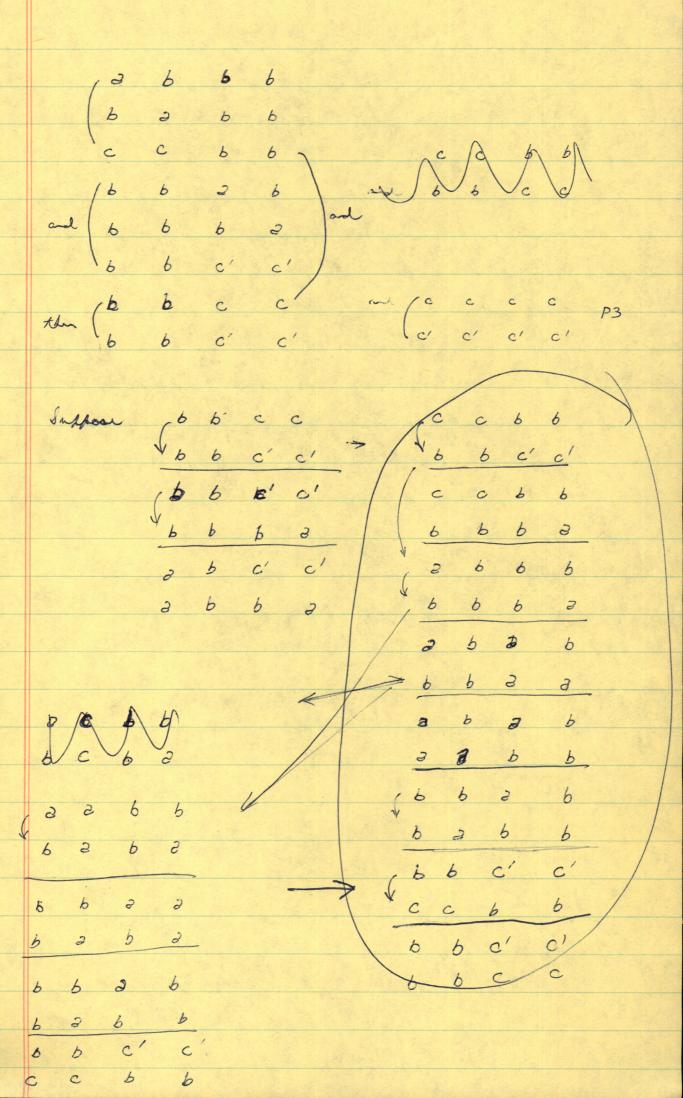
i.e. "the difference "butwern II and (I, II) can never "make."

a difference such that" buth I > I and I > II; i.e. in any pair

(unless II = X) involving II, with I could be substituted for II without effecting ordering, on III could be . (i.e., if II > X, then either I > II > X or I = II > X or I = II > X. of I<X, ith I < I < X on II < I < X, or I = I = I < X. BUT unspore that for some E, II > I and II > II. Then it night be that I > X > I and I > X > II, 40 In this case, different would "make a different"; mitter much of the set (I, III) would be an assistable substitute" for IL. Columne: If you may math expect with weights, an wights must not sold to > 1; or else Amphore Ep. = K >1 = 1 = 1 = 1 V(I)=1 v(II)= - (Ep:)=1 But suppose Ep: <1 Ep=k<1

- (2) A for all X and all E.

det I i II i II per some E. Then for any E, III = III IT I 2 6 TI C C I C' C' asum 2 > c > b and 2 > c' > b Suppose C'> C. Jan TV > II Then I > III and II > III 1) 2 6 and 3) 6 2 2) C C 4) C C  $\begin{pmatrix} c & c & b & c & b & c & b & b & c' & b \\ & b & c & b & c & b & c & b & b & c' & b \\ & c & c & b & c & b & c & b & b & c' & b \\ & c & c & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b & c' & b \\ & c & c & c & c' & b & c' & b & c' & b \\ & c & c & c & c' & b & c' & b & c' & b \\ & c & c & c & c' & b & c' & b & c' & b \\ & c & c & c & c' & b & c' & b & c' & b \\ & c & c & c & c' & b & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b & c' & b \\ & c & c & c & c' & b \\ & c & c & c & c' & b \\ & c & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c & c' & b \\ & c & c' & b$ (3 6 6 8 c' c' CC



Suppose for som E: 3//6 (a) (c) S (c) Suppose 3 6 6 3 C C (d) P P -S 0 (d') and (d d' c c d' d -P and of d d then (b c d' d' Proof: Suppose d' d' d' d' d' ac Suppose jb c

b c b c d' d'

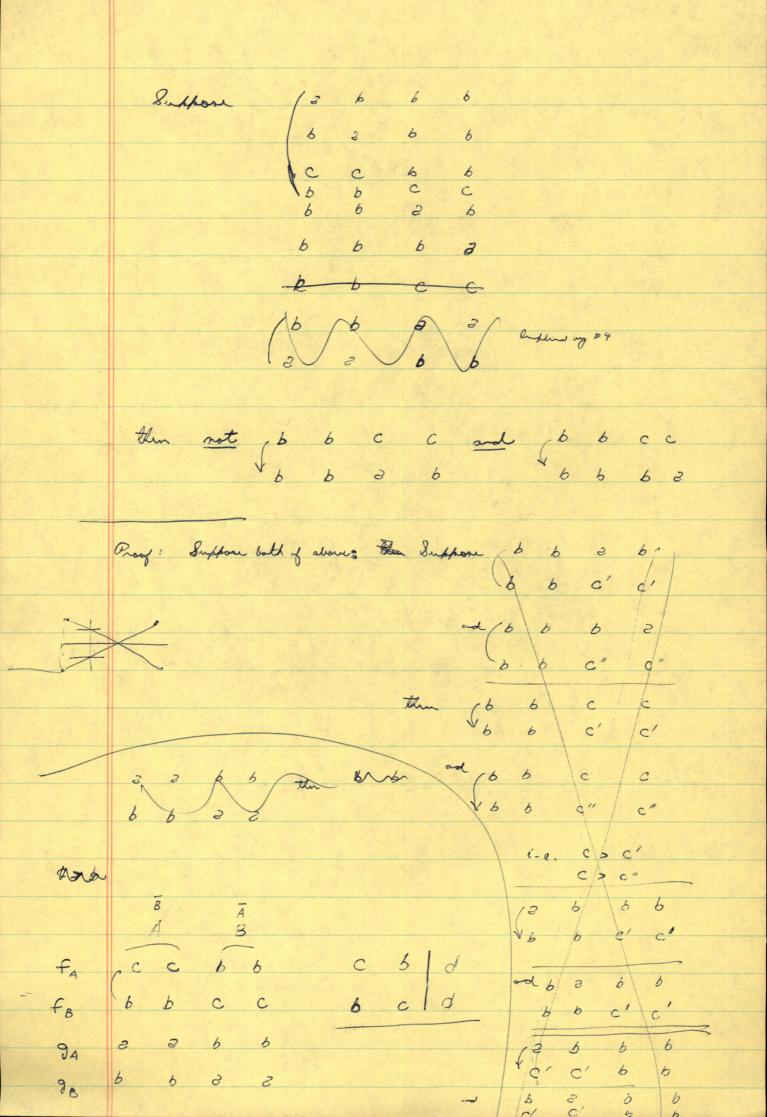
d' d'

b b b b b c c c

d' d'

d' d'

controlier la 2 5



ad ( b b c c c ) Proof: Suppose 1 6 C C (then for a 02/26 5 6 (c c b b 2/6 c e c b b 2 2 ( com c c D (b b b 8 c c 5 C ( b 6 b b ) 6 8 \_ c 8 2 3/6 3 8 2 8 3 C C 5 8 5 8 cont. \$ b b C 6 C

## THEOREMS

TH D By P4: (I 2 2 6 6 6 II 6 6 2 2

II C C 6 6 Thm

II 6 6 C C

2>6>6

I = I 😂 II = T

see Savage, 1.31

Proof: I, II, II, II ; and A, B; 3, 5, c, it; are much that

(22) I = 2, II = C for  $\mathcal{E} \in A$  I = b, II = b for  $S \in A$ 

(26)  $II = \overline{J}$ , IV = c for  $S \in B$  II = b, IV = b for  $S \in \sim B$ 

3. I= I

The lay P4: II = II

TH. 6: T b z b b

T C C b b

T b b c C

T b b b c' c'

T b b b b b b

T b b b b b

Th: if I=II=II = IV, and I-II=II ; then I=II=II=II=II=II ed c=e'

Proof (): D=XI=(2) II = II = II = II, when III 2 2 6 6 ly Th. 1. TX 6 6 2 2

(b) I = II, II = III, III = III = III = III = IIIluy proof in my article, Th. O.

c) Hence IV = I (= I = II = II = VI = VII) ly PI

Proof (2) Suppose TE b b C C IY > I 2 6 2 6 PI (thim II = IV and Theorem 1) b b a b b P2

b b c' c' P1

b b c c c'

CONTRADICTION

Theorem 3,

CONTRADICTION

It: V = T = T = Tthe not both T > T and T > T(i.e. with T = T or T = T, or both, in which can T = T = T)

(or: with T > T > T or T > T or T = T = T)

Theom (9) T 2 6 6 6

T 6 2 6 6

T C C 6 6 ~ (II 2 3 6 6) \( \tau \) 6 6 2 2 \( \tau \) I c c c c / JA: Y I= II and IV= V, then IV= V= U Proof. 3) I 3 6 C C) W 6 2 c c Mccccc/ VI = VII = VIII by PZ b) I 2 b b 6 T C C 6 6 52.1 b b c c N 2 2 6 6 P2 M 9 5 C C

This: "How much should I pay for a but: 10 00? Suppose E is: Lighty andiques answer (Savage): 3) The your indeffent between b) If so: pay up to amount you would pay for H T 10 0. of "but" is -10 0; ask no more than if but were Suppose agent looks into un I and tells you: either A (proportion of Red is between  $0-\frac{1}{3}$ ) or B (" " "  $\frac{1}{3}-\frac{2}{3}$ ) a C ( " " = " = 2 -1). Suppose de says: "B". Rospe: UI UI 50:50 (1) i R b (2) i R b i b R e 3 2Rb i 2R b? & not, contradiction ( Need not sur offer 6R, 2 vs 6R, 2)

Flyhility: (see Mandel- Moon)

Set 3, determine the set of actions at  $t_2$ .

2) actions at  $A_2$  should be characterized by objective outcomes; because one verson for flexibility is that payoff function (strategic objectives) may change between t, and  $t_2$ .

2, more flexible than  $z_2 \Leftrightarrow A_1 \supset A_2$ .

6)

Suppose payoff for will stay same from t, to tz. The actions characterized by payoffs.

It may be that payoffs to "som" actions are lower if closer out of Az than act of Az. Then A, doesn't "include" Az, if we characterize action by payoffs.

But it may be possible to arpuset payoffs to action as  $\vec{z}_{i} = (\vec{x}_{i}) = (\vec{x}_{i})$ , where  $(\vec{y}_{A_{i}})$  is a vector depending on the set  $A_{i}^{c}$  (determined by  $\vec{z}_{i}^{c}$ ) and independent of the action  $\vec{z}_{i}^{c}$ ; and  $(\vec{x}_{i}^{c})$  is a vector depending on the action  $\vec{z}_{i}^{c}$  and independent of the set  $A_{i}^{c}$ .

In patienter, assure (y') is a constant vector.

The it represents the "cost of closing from A' ."

(y')-(y') = ipportunity cost (right) of closing from A' rather than A' . (assure y' > y").

Special case: y' > y " (objined objecting).

Say 3, is more flipible than 3, " if Az DAz" when actions an shareterized by the payoff vectors (xi).

## Sprint con! (xi)= o for all is

Special case: assure y'= 0 for all is mad That Az' consists of one action only (no close possible at itz; only choice is is, at t,).

Value of flex. is not related to the amount of info of report to gain between t, and to bet the value of info of 'expect' (conservating').

High: How much I will pay for flex. is related to antiguity of my expectation on value of info to be gained.

 $A_{2}^{i} = I \quad 0 \qquad A_{2}^{m} = 0 \quad I$   $\equiv 0 \quad I$ 

Thus, if 2, 42, 2, 42, 2, 5, 42, 2, 5 A2, 3, 5 A2, 5, and will proper of to 2, 6 and will for prime of to 2, 2, and though (if it look been offered) he would have been idefferent between 2, 6 and 2, 7 ; and would have been idefferent between 2, 6 and flipping a coin between 2, 6 and 2, 7.

When the effect of appoints strategy or my pageffs is only way to know "what he did," the hedging strategy scripin classery gaining info during seguritial process.

(" you can't see the conds meles you pay." (Suppose you don't "see"the even them, but impies areans unlittle you were bester or not. Knigspiel.)

Flexibility: Define physical auteone—"state of the world,"
relevant aspects — in terms of or dimensions. Specify relevant on
contingeness, states of the world that affect auteones.

An action maps a state of the world into consequences.

A set of actions is larger than another set with repert to given contingency (state), of and with respect to m divinsions of author, if for that contingency, the set of different values of the m dimensions "available" within the set is larger; in fecticular, if it includes the ather set.

Since the costs of different actions may be different under different sets, define "availability" w.r.t. a fixed budget at the time of choice. This, set could be more flyible than set B at a dight budget, but his plyible at a low budget.

Value of flexibility will depend on: 1) exact notice of uncertainty about the state of the world; 2) various costs of uncertainty expected to prevail at t2, time y cloice. 3) passible variation in payoff function; 4) aution payoffs to less flexible alternative actions or sets of actions.

Close of an action at time to rules out further close, further control; it includes choice of a decision rule for acting on further impo

Promethat for any  $E \ni I \ni b$  I : I = II, C' = C  $I b \ni II c' c'$ 

Consider either

2) Back A many lot 2 Back B co experient E Back A + B through to prototype A is chaper of Dis chaper z, outcome of e, favorable to 6,

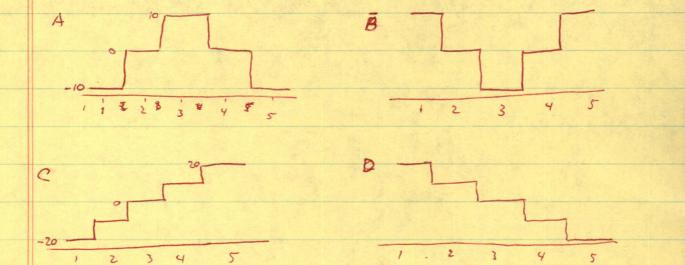
If we assure payoff function fixed, the : 2) can define flyibity in terms of different payoff; so set of actions "available" under given contingues will be smaller (some physical actions will be seen payoff); (6) can count only undominated actions in set, w.r.t. whole set of contingues on w.r.t. some subset of contingues is (1.8. 2 event; or even 1, if walnuss are defined only so a partial ordering) in evaluating a set of actions.

Thus, if a "large" set of actions A has a single dominant strategy a'', a'(A) = v(A'), when A' = a' (less flipible).

i) N/m does A > B => v(A) > v(B)?

2) for to measure "value of fluidity":  $v(A) - v(\partial')$ , where  $\partial' \in A$ ,  $v(\partial') \ge v(\partial'')$  for all  $\partial'' \in A$ .

(w.r. t. "least flipble subset" of A).



(1-5 are dish settings; A-D on events, or different payoffs functions; graphs are

bayoffs)		A		_						
		A		4	20					
	1	-10	10	-10	20			-		15
	2	0	0	-10	10	10	10	30	10	15
	3	10	-10	0	0	0	20	20	20	15
	45	.0						10		15
THE RESERVE OF THE PARTY OF THE						20	0	0	40	
	5	-10	10	20	-20					

margine Value of fleribility:

copte expected right of man proming some subset of (n-1) actions, us, set of n actions.

1-	5:	10	(0	20	20					
1-	4	10	10	10	20	0	0	10	0	2,5
									11	
2-	-5	10	/0	20	10	0	0	9	lo	2.5
,	3	10	10	0	20	0	0	20	6	5
- 1	3	/0			20			20		,
3-	5	10	10	20	0	0	0	0	20	5
2.	4	10	0	10	10	0	10	10	10	7.5
14	5	-10	10	20	20	20	0	0	0	5
		1-								
24	3	10	0	6	10	0	10	20	10	lo
4	-	0	10	20	-10	10		0	30	do.
7 7	3	O	10	20	-10	,0	0	0	30	46

2-4 has higher arrange right than (1,5).

If  $A\supset B$ , you must do at least as well with A as with B for any contingency. But have  $V(B) \leq V(A)$ . Expected right for B  $\geq \frac{2}{2}$   $\leq \frac$ 

But if, say, two actions within the sent had, butween them,
the best payoff for every contingency, there would be no walve in
adding now actions. Never a walve in adding an action unless
for some contingues it is best (assuming you will know event with
certainty before acting).

Therelishing is a way of lowering expected regret. If a single action were available with some regrets as 1-4, it would be just as good. You can't till just by looking at a sets of payoffs corresponding to two strategies, which is more "flexible." (exp. if cost of flex, has been subtracted).

THE THE PARTY OF T

IOIOIOI I I O I O I O assure rest, dist. Value of I.  $v(I) = v(I,I) = \frac{1}{2}$ Value of info that event is (1,2), (3,4) or (5,6) = 0 Value of info that event is (odd) or (even) = - ?. Value of flexibility when you expect benfut info = value of perfect info = expected regret with less flexible set compared to more flexible set, who you expect perfect info later. Value = f (info, flex). Value of info: (1,2,3), (4,5,6) = 6 Suppose of start knowing: (1,2,3)  $v(\mathcal{I}, \mathbb{Z}) = v(\mathbb{Z}) = \frac{2}{3}$ Value of info: (1,2) or (2,3) or (1,3) 1. 1 + 1 : 2 + 1 : 1 = 3. Value of info = 0 But if & start with (1,2,3,4): V= and learn (1,2,3), (2,3,4), (1,2,4) or (1,3,4): v: 3 Value of info = 6 On: start with (1-6), go to (4,2), (3,4), (5,6): valuey info on flex = 0 [go to (1,3), (2,4), (5,6): waln y ife = 3] But start with (1-4), go to (odd) or (even): walnut info = -

See Marshel + Nelson, p. 9

1 2 3 4 5 6

For flipebility to have any "value", it is necessary (but not sufficient) that either (0) expectations - may change, as a result of new info or further analysis; or (6) payoffs may change, as a result of new info, or analysis, or 'leaving," " to.

(Ether For either of these, it is necessary but not sufficient that initial expectations and/or kayoffs be uncertain).

Whith give flicibility will appear valuable, and to what degree, will depend on 5 e.g.: 1) the forcise way is which it is believed that wentarity will be reduced or clarged (e.g. new ip, of greater reliability then initial info, may simply continuent cost doubt on continuity of a common on Mans, cross-examination of interesses, general strategy of defense (of a client who doesn't have closent knowly of imposement).

2) the payoffs to the various inflighted alternations, and to the closes permitted by the flighted strategy; e.g. the costs of flighting.

3) The lead time of the info of given condibility and the speed of vaporase (BNEWS).

Flexibility is a form of insurance (not vive versa) primised on the possibility of acquiring valuable information; its value is equivalent to the expected (or index) value of information for the flexible set of actions as offered to the expected value of some less flexible set. Other forms of insurance can be evaluated on the assurption that info does not change or infrare (e.g. that it worsens) or that true clove will not be made; i.e. that initial chaire will "wall," obtaining action.

Mining right could be interpreted as:

Way of evaluating 3) flixbility, assuing perfect info at  $t_{i}$ ; on 6) perfect info, given flexible set at  $t_{i}$ ; when no restriction can be fet on "mosorable" probs, and X = 0 (p = 0).

Af flogible action of "cost" of flexibility is independent of actual went which obtains, flexible actions out of articles will have constant right w.r.t. less flexible set (This does not guarante minimax right where cost is 0; does it?.

Ele evaluating value of info, with give flexibility; with "fixed"

cost of info.

Suppose there is a possibility that wenterity will not decrease, I am a small prob. That it will increase (that signals may occur increasing wenterity). Flexibility per see won't "insure against" this possibility. "howeve" actions "look amptable" against initial or higher montainty. Include them in physble set.

ANN stresses.

Decision to drop 2 bombs on Japan, before text. (Decision could have been segmential, flexible, but wasn't).

Difficulty of wally "postformy decision"— "leaving alternatives open"

Flacture offusions, "Cost" of smitching from "publicly expected alternative

on of "delaying decision" may be such as healty to drop out certain

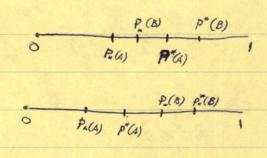
alternatives from fixed-budget comparison.

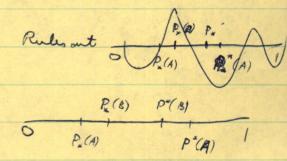
$$P_*(A) \leq [1-q_*(A)] = p^*(A)$$
 $P_*(B) \leq [1-q_*(A)] = p^*(B)$ 

P2: 
$$p_{*}(A) > p_{*}(B) \iff q_{*}(B) > q_{*}(A)$$

$$p_{*}(A) = p_{*}(B) \iff q_{*}(B) = q_{*}(A)$$

$$p_{*}(A) < p_{*}(B) \iff q_{*}(B) < q_{*}(A)$$



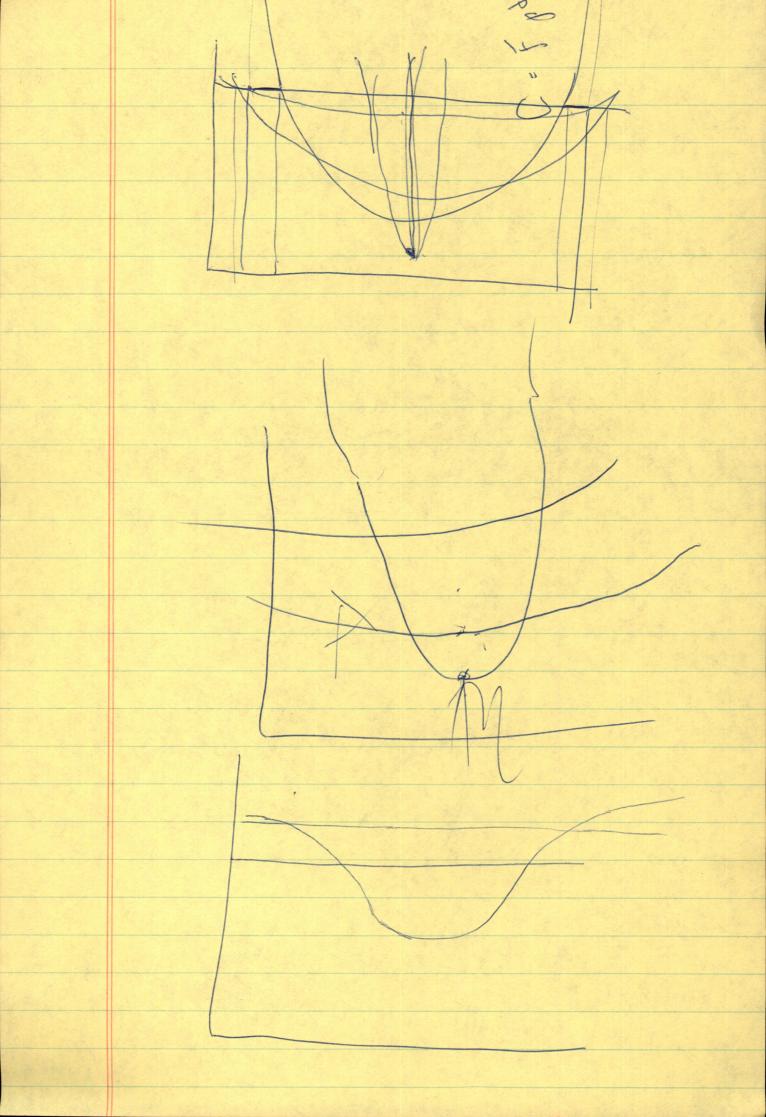


$$0 \quad 1 \quad 0 = 1 - 9_{*}(B)$$

$$1 \quad 0 \quad 0 = 1 - 9_{*}(A)$$

$$(1 \ 0 \ 1) \le (1 \ 1) - (0 \ 1 \ 0) = (1 \ 0 \ 1)$$

$$v(1 \ 0 \ 1) = \frac{1}{2} \le 1 - v(0 \ 10) = 1 - \frac{1}{6} = \frac{5}{6}$$





1 0 0 3 -1 0 0 -1 0 1 1 0 1 1 1 6 6 P\_(A) P\_(A) P\_(A) 9\_(A) 9\_(A) 1 0 1 0 1 6 9 (B) 9 (B) 9 (B) P (B) P (B) Colume: \$ (A) \( \rightarrow (A) \( \lefta \) V(100) & 1-v(011) (Savage wonts to prom their equal) -100 v(-100) = v(0 1 1) - 1 = - p\* -p\* -p\* so 9-p\* = = 9x(A)-1 or p\*=1-9= To assume px = p\* is to assume px = 1-9x and to assure v (100) = 1- v(0 11) (or to assume v(100) = v[(111) - (011)] 11/1000 v(100) = v(010) ⇔ v(101) = v(011) v(100)-v(010)=v(000) => v(101)-v(011)=6

(1-10)=0

JA 5 ? E E

I (1000

II (P) P 000

II (0100

II (000 9 9

II (000 P' P'

III (000 100

Then p'=p, T=TT=T=TT(i.e. gime that p=1-9 for some E, and gime p', g' for event F, with p=p', then p'=1-g', g'=g

By  $\stackrel{P2}{=}$ , if  $p_* = 1-q_* = p^*$  for some E, this must hold for all E' such that  $p_*' = p_*$ ; because by P4, if this inplies  $q_*' = q_*$ ; as if  $p_* = 1-q_*$ , then  $p_*' = 1-q_*'$ 

(But what guarantees that this ever holds? P5:3)

P2 gives complete andering, but descrit guarantee that  $p_* = p^*$ . It does however, if there exists any "definite" p corresponding to every went  $\partial p_* = p$ .

P2 rules ant one "internal" enclosing another.

D. yo + 1-p [x. (ymox - yo) + (1-x) [ymi - yo]]

I= \( \frac{1}{3} \) I=

Rayling II-II, IV-III

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their waing minimage regult or in his using it to resolve their reported disagreement.

Hyp: Where minimax regret looks good to an individual, it is in circumstances when it looks good on Ellaburg index; and in such cases, (in all cases) some other action may look better. (may have higher max regret, but ... higher minimum, or higher may, or higher Xest).

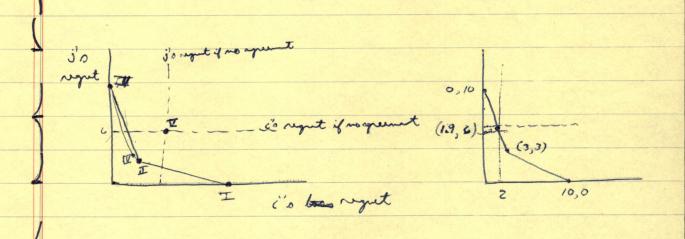
For group,

a pendicity of this bangering situation is that acts an available — involving observations — with way low regret.

Regrets happen to express relevant payoffs in certain problems.

But strict mining is no now generally valid with regrets then with losses.

i j
I +10 0
II 3 3
III 0 10
II 2 345
Doubt ague \$\overline{\pi}\$ 5 6



One who "caus less" if no aprement is recited is information the baryoning position "to influence actions within the acceptable set (What if he makes threato to fail to agree?)

Bj Br

I O -14 4 believe  $(B_1) = 1$  (not one),

II -3 -13 Experted loss to III = 1. But max loss

III -1 -20 to II = 10, where so max loss to II is

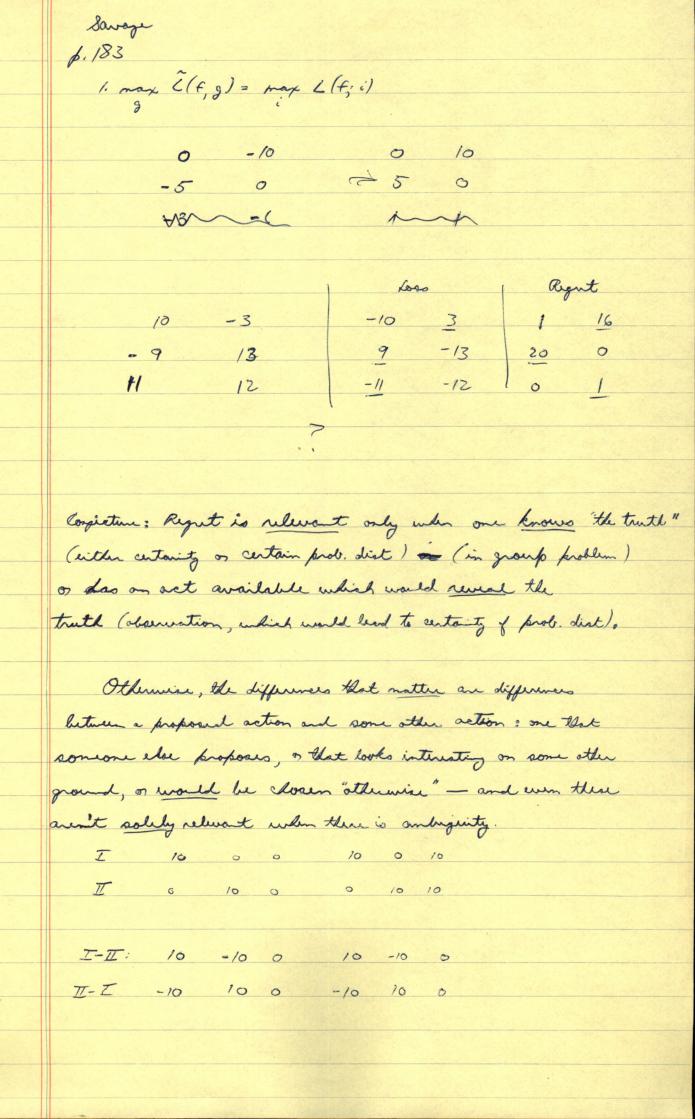
II -4 -10 3 (which is also expected loss to

Dee lawage, p. 159.

of \$4: looks lutter than I (the max loss is not enough worse to arturish)

Da gane: I 10 Person who preferred either mixed strats (1,0,0) or (0,0,1) to (0,1,0) or to (1-1), 1, 1-1), 0 \ 1 \ 1, will 2) be disobering favoge axioms (as is missinger; but for different b) be following Ellaburg rule with & > 1 (more weight to "good" ambiguous possibilitie than to bool ) c) also prefer any non-symmetrical mixed strategy to any number of ( 1-1, 1, 1-1).

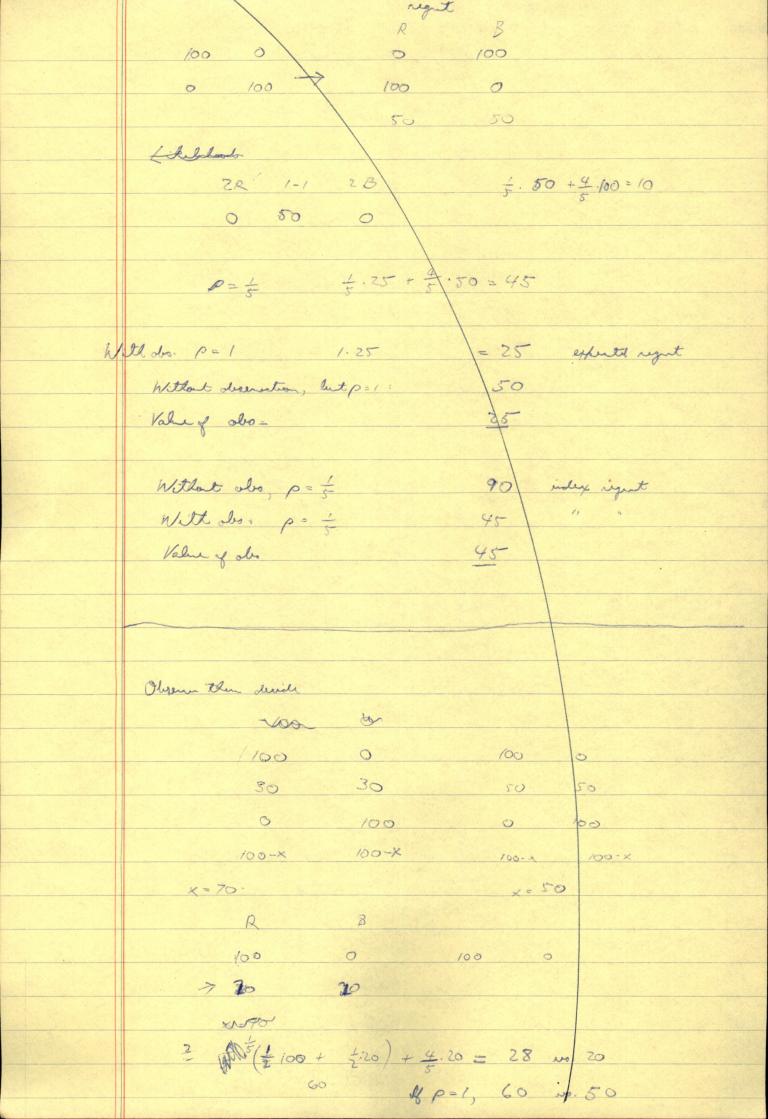
10,20 19,20 29,10 20,10 20 - 18 Dung D 0+20 -8 + 10 Huse P -8+20 0 =10 12 -10 30 60 with all B, on 30R, 30B R Ros 30 60 with all B on 30R, 30B 30 R R B 0 -8 0,-8; \frac{7}{3}-\frac{2}{3} 0 -8 0 0 0 -8;  $\frac{7}{3} - \frac{2}{3}$ 0 -8 -8 0-8; 1 -8 0 9-8; 5-2 -8 -8 / / 0 0 0 -8 0 -7 9 -8 8 Not equivalent -5 11



RYD Don't produce o 0 Without observation, Don't produce to Produce -106 100 Observe, then decide: -100 100 Possible usulto of observation: T 1 0 1 of -100, I want produce; payoff 0; deference to of 100, Oroduce; payoff 100; difference 100 V & absenction, \$\frac{1}{2}.0 + \frac{1}{2}.100 = 50 I will pay up to 50. **★** -100 100 -/00 /00 Observe, the deside F100 160/ A B Dayoff -/00, -/00 -> -/00 \frac{1}{4} - 100 100 100 · 100, -100 100 4 100,100 100 4 V(dos) = ( 1 . -100 + 3 . 100) - ( 2. 100+ 2. -100) 50 - 0 Divinoper: to Payoff t absuration: Xest = 50 X = -100 X = 100 p= 3 X= 6 \$.50+2: loa = 25 3.50 + 4. (100) = 12.5 A: 4(50) + 4. (-100) = 12.5

100, -100 100 -100, 100 100 100, 100 - 100 -100, -100 -> 0 Hale of abservation estimated: 75 -75-0 = 75 Bondy, p= 4, x=0 1.75 + 3.0 = 18.75 Andley to A: 4. 50 + 3. (-100) =-62.50 81.75 35 4 75 4 4 I .100 T 0 100 Index: P= \$, x=0 = \$\frac{1}{4}.50 + \frac{3}{4}.0 = 17.5 Value of observation = 100 - 12.5 = 87.5 Un Index: p=1: 50 Value of observation: 100-50 = 50 On if observation will produce prob. dest: OR, 2B 1R, 10 2R, OB 100 50 100 9 5 37.5 4.(75) + 3.50 = 56.25 18.75 Value of also \$ 56.25 - 12.5 =

```
Un I - 2 ballo. 2R, 1R.1B 2B
        V<sub>I</sub>
               R B
Don't but I
             X in X
        II 100 0
              p= 5 X=0 Yest = (1, 1)
        ·(UE) = $ . 20 = $ . 40 = 10 ($ x < 10)
          In U, allow observation of ballo, then closes of I of II:
                  ZR 1R18 28
                 100 50 0
              £·(25+25)+ £.0 = 10
         I 6 0 0 p=1: v(I, I)=2
         I 0 6 0 With abo; v(I,I)= 1.6+1.6=4
                                 Value of obs: 2
          \rho = \frac{1}{2} \times 20 \quad \nu(\pi) = 1, \quad \nu(\pi) = 2, \quad \nu(\pi, \pi) = 2
            With observation: V(I,I) = 1.4+1.2 = 3
        # Value of observation = 1
        TT 6 0 6 p=1: v(II, IV)=4
        W 6 6 With also: V(III, III) = 6
                             Value of obs: 2
         \rho = \frac{1}{2}, \alpha = 6. \nu(II) = 2 + 1 = 3, \nu(IV) = 4, \nu(III, III) = 4
                With obs. v(III II)=6
                 Value of obs = 2
```



```
I 100 0
                         yest - (2, 2)
        I 0 200
         p=1: v(I)=50, v(I)=100, v(I, I)=100
              WIR obs: 1.100+ 1.200 = 150
                Value of obs = 50
         P= 2, d=0 VIII = V(I, I; 1/3, 1/3) = 66 /3 XMAN
                 With obo: - 150 + 1.50 = 100
                Value obs: 333
         P= 1/2, Yest = (5/3/3) == pr(R)=1/3
   T = 2\frac{1}{2}\sqrt{T} = 3, v(T) = 3, v(T) = 3
         TI 6 0 6 value of obs: 6
                          value of obs. = 3
  424
              & P=1: V(II)=2, V(II)=4, V(II, II)=4
600
                   With obs: V(II, II) = 6
                   Value of obs = 2
066
3 3 3
             If pr (R) is also antiquous:
              V(II)=/
               V(II)= 1.4+1.0=2
              v(T, T52, 2)=3 with obs: 6
            Value obs 3
               all probs ambiguous
         I 6 0 6
                                3 3 0
         II 0 6 0
              V(I) = 1, V(I) = 1, V(I, I; -1) = -2 \cdot 2 + -2 \cdot 0 = 1
              With abo: 1.4+1.0=2
             Value of obs: 1
```

info would go up, because he would expect walnute info. moral: if outcome will still be antiquous after observation, "conservation " will pay less for observation than Bayesian, because he is less sure of getting valuable info. But if info will transform on antiquous statution (all alternations andiquous gambles) into risk or certainty, conservative will pay mon for info; value with also. is same as for Bayearian, but walve without info is bear. R ( show would be worth more to conservative if he couldn't use mixed attack). P=1: V(II)= v(II')= 2 With obo: V(II, II') = 4 T 0 0 6 p= = = , pr(R)= = = . v(I, I, 2, 2) = 2 With observ. : V(II, II') = 4 8 8 0 8 8 V(A, B)= 2.6+2.4=5 V(A,B)= 2 8 = 8 With do = 4 0 0 8 0 Vogobs = 3 To Bayesian, waln obs = 2)

I 6 0 0 P= 2, X=1 T 0 6 0 v(T) = 2,  $v(T) = \frac{1}{2} \cdot 2 + \frac{1}{2} \cdot 4 = 3$ With also, V(I,I)= 2.4+2.6=5 Value of also: = 2 TT 6 0 6 T 0 6 6 V(III) = 2.4+2.6=5 v (17))= 4 With obs: 6 Value of als: 1 "Optimist" put value of problem without info as higher than conservation (or Bayesian); and protestalangings but since there is a cailing on to value of problem with info, he may walne info less than either conservative or Bayesian if ceiling is reached; he will value to info more than conservative if ceiling is not resolud. R PB R PB In case: # 606 II 0 6 0 TO 6 6 M 6 0 6 when conservative values info more than Bayesian (3 vs. 2), conservative doesn't know whither Y is more or leas likely than B, don't be know they are exclusive. Consister man who doesn't know whither expected value of III is O or 6 and doesn't know whithe expectation of II is O or 6 but he does know their correlation of outcome; when pageff to IT is 6, payoff to Tio O, and vice wears ; hence an observation, which 8 8 8 will tell him which state applies ((Y) or (R,B)] will guarante him a payoff of 6. Hyp: parallel paths pays non to conservative

Than to Bayesian ) if he knows outcomes are negatively correlated.

Regrests measure the value of various possible missages about true state of the world, relative to a given action. There is no reason to minimize the max of these. At: Coules De Fondation Dige . Paper